

## SET 9

- (1) Show that if  $a$ ,  $b$ , and  $c = a + b$  are positive integers such that  $ac - b^2 = 1$ , then  $a$ ,  $b$ , and  $c$  are consecutive Fibonacci numbers.
- (2) If  $P(x)$  and  $Q(x)$  are non-constant polynomials such that  $P(P(x)) = Q(Q(x))$  (as polynomials) and  $P(P(P(x))) = Q(Q(Q(x)))$ , does it follow that  $P(x) = Q(x)$ ?
- (3) What is the largest possible number of acute angles in a polygon which is not self-intersecting (no two non-adjacent edges intersect)?